

Ultrasound image Uniformity Assessment by Means of Sparse Matrices: Algorithm Implementation and First Results

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Abstract – The current study is focused on an image segmentation algorithm for Uniformity Quality assessment in Diagnostic Ultrasounds. In particular a mathematical definition of the uniformity in ultrasound images is introduced and a split and merge algorithm performed on sparse matrices to measure uniformity is described. The algorithm is based on the Gray-Level Co-occurrence Matrices and the related descriptors, i.e. the Haralick features Entropy, Energy, Maximal Correlation Coefficient and Information Measures of Correlation. Results on 2 different datasets of test images with different non-uniformities have been carried on. Several outcomes show a good sensitivity and agreement with the mean judgment by 7 human observers, i.e. differences are below 40% in most of the cases. On the basis of previous studies, the latest developments and results are proposed and commented.

Keywords – *Uniformity measurement, ultrasound, speckle, Gray Level Co-occurrence Matrix, Haralick features*

I. INTRODUCTION

Today diagnostic ultrasound (US) systems are a powerful and widespread technology of medical imaging because of their ability to provide real time images with good resolution and no risks related to ionization radiations. Further advantages are versatility, transportability and costs usually lower than other medical imaging technologies. Since the diagnostic decision is based on the digital image from the ultrasound scanner [1], it can be considered as the starting point of the quality assessment of the whole medical device [2]. In literature, among many image quality parameters investigated [2-5], the uniformity is often considered relevant, as in other biomedical fields and technologies [6-8], even if its evaluation seems to be often subjective and not univocal [9], usually performed by specialized technicians without standard criteria: therefore, results are not univocal, depending on testing devices, settings and operator subjectivity [10].

Indeed, automatic systems and characterization procedures that can support the medical diagnosis are always in developing [11-14]. A recent approach to uniformity objective quantification applies pattern recognition and image segmentation to the ultrasound image provided by ultrasound phantoms [15]. In particular, the uniformity into a Region of Interest of the ultrasound image (ROI) is defined as a measure of the diagnostic system capability to display the speckle of a tissue in a homogeneous way within the ROI [15, 16]. From the definition above, the number and dispersion of different textures in the ROI is required to calculate the ROI uniformity index: the higher is the number of textures in the ROI and the differences among them, the lower is the ROI uniformity. Several methods in literature studied speckle to either reducing it [17,18] or identifying and characterizing speckle patterns into the ROI [20, 21]. This is based on particular sparse matrices, the Gray Level Co-occurrence Matrices (GLCMs) [19], and is characterized by some mathematical operators, the Haralick features. In particular a GLCM is a bi-dimensional histogram where spatial correlations among the grey levels in the ROI are expressed: for all the pixel pairs in the ROI, that are separated by a Inter-Pixel Distance I_{PD} along the orientation θ , the value of the matrix element (p, q) is the number of times that the grey level q occurs after the grey level p. The GLCM is usually normalized by the total number R of paired occurrences, so that from the normalized GLCM $\Phi_{1,\theta}$ the texture information is extracted evaluating a set of the Haralick features [19, 20]: for a same I_{PD} and θ , similar textures are characterized by similar sets of values, since the Haralick features are related to different image characteristics, as contrast, brightness, homogeneity and complexity of grey tones spatial distribution, and in the scientific literature there are many examples where they are applied to texture recognition and analysis [19-23]. Nevertheless, although the US image uniformity quantification can be very useful for both maintenance and research purposes, the application of GLCM and Haralick features extraction to US image quality assessment has not been yet widely applied. To this aim, after a brief overview on main me-

thods and results in literature, some theoretical elements and improvements of the method in [16] are illustrated and its application to images provided by commercial ultrasound scanners is proposed: measurement results are reported and commented. Future developments are finally discussed.

II. RELATED RESULTS IN THE LITERATURE

Studies on methods for image uniformity objective measurement are quite common in literature, even if their application to ultrasound image quality assessment is less investigated, since subjective methods are the most widespread [2-3,9]. In Hangiandreou *et al.* [24, 25] in-air images and speckle images of a uniform region of a ultrasound phantom are visually inspected: vertical dark bands (axial hypoechoic artifacts) usually indicate a localized transmission/reception failure. On the other hand, in Martensson *et al.* [26] a probe tester is proposed for the relative sensitivity measurement of each piezoelectric element of the ultrasound probe: defective channels were found by means of the objective evaluation of the local sensitivity. Another computer based method is reported in [27-29], where the uniformity of the echosignal or noise is evaluated by imaging a uniform region of ultrasound tissue mimicking phantom and an in-air-image respectively: the averaged signal pixel values at a given depth are plotted as a function of the scanning direction and a local decrease of a few dB or more may indicate system failures. In [15], the image gray level histogram of the ROI is weighted by sigmoid functions to determine the spread of the image histogram due to non-uniformities. Anyway, all the above approaches have been based on a first order statistic of pixel values into the ROI, while in [16] the correlation between pixels is used to determine the speckle pattern characteristics and homogeneity to quantify the ultrasound image uniformity: this approach is described in detail in the following sections.

III. DESCRIPTION OF THE METHOD

In the first two sections A and B of this paragraph the definition of the ultrasound image uniformity and the input variables criterion are reported. The third section C examines the block-diagram of the algorithm proposed. Finally, the last paragraph D explains the datasets used.

A. Uniformity: definition

The definition of image uniformity is based on the principle that it is possible to define a segmentation criterion to divide the image into areas that are characterized by features that differ significantly from those of the adjacent neighbors: two adjacent areas with similar (or equal) features are considered uniform (therefore both of them belong to the same area). Sometimes segmentation is made easier when it follows some foreground extrac-

tion technique [30]. The image uniformity is measured from the number of ROI partitions and the quantification of their difference after the segmentation process (split & merge algorithm), to this aim a set of features (Haralick features) are evaluated over the whole image and its partitions. Therefore, a preliminary choice of the image features should be done, since the segmentation process into regions depends on the chosen features. In [8] the image uniformity is defined as:

$$U_{ROI} = 1 - \Gamma_{ROI} \quad (1)$$

the non-Uniformity index Γ_{ROI} in (1) depends on the image features. The dispersion (i.e. standard deviation) of the sub-ROIs characteristics at the end of the segmentation process is used to measure the ROI uniformity $U_{ROI, I_{PD}, \{f_1 \dots f_k\}}$ [31], as each sub-ROI corresponds to a specific set of several GLCM feature values f_k as well as textures:

$$U_{ROI, I_{PD}, \{f_1 \dots f_k\}} = \left(1 - \frac{\sigma_{\{f_1 \dots f_k\}}}{\psi} \right) \cdot 100 \quad (2)$$

Where $\sigma_{\{f_1 \dots f_k\}}$ is the standard deviation of $\{f_1 \dots f_k\}$ among all sub-ROIs and ψ a normalization coefficient, adapted from [31]. In the algorithm developed the $U_{ROI, I_{PD}, \{f_1 \dots f_k\}}$ can be evaluated for more inter-pixel distances I_{PD} : in that case the final value of the image uniformity U_{ROI} is associated to the minimum of the $U_{ROI, I_{PD}, \{f_1 \dots f_k\}}$. For a same ROI, numerical results mainly depend on (a) orientations and (b) distance I_{PD} in GLCM calculation, (c) the GLCM features f_k , (d) ROI size and position (e) threshold values (split and merge) for f_k discrimination between not homogeneous sub-ROIs [16].

B. Setting Input variables

The most important input variables here considered are: (1) features type, GLCM (2) directions and (3) inter-pixel distances I_{PD} , (4) the threshold values of the differences between features of adjacent sub-ROIs for the segmentation criterion, i.e. differences above the thresholds are associated to sub-ROIs of different textures.

From other studies performed by the authors the following Haralick features have been selected: *Entropy* (f_1), *Energy* (f_2), *Maximal Correlation Coefficient* (f_3), *Information Measures of Correlation II* (f_4). Every feature above is evaluated on GLCMs obtained for the two directions, $\theta = 0^\circ$ and $\theta = 90^\circ$, at a specific inter-pixel distance I_{PD} . With this aim a Fast Fourier Transform (FFT) analysis on each test image has been implemented for both directions to determine the I_{DP} from the frequency of the first peaks detected in the corresponding FFT spectrums by means of an adaptive threshold algorithm: in order to reduce computational complexity, only one I_{DP} value is here selected for each direction in the test image. In particular the adaptive threshold algorithm finds the first

FFT peak in a spatial frequency interval where the minimum is related to the ROI size and the maximum is dependent on both the ultrasound scanner spatial resolution and the operator visual acuity. On the other hand, the optimal threshold values for the segmentation criterion (split and merge algorithm) have been estimated for each feature on a speckle test image, assumed as uniform and evaluating the U_{ROI} at different threshold levels (range between 0 and 1): for each feature the optimal threshold is determined in correspondence of the maximum uniformity U_{ROI} .

C. Block-Diagram of the sparse matrix algorithm

In this section, the block diagram of the method proposed is described (fig.1). The code has been implemented in a MatLab environment (Matworks 2014), with functions based on the use of sparse matrices. In particular, the image (ROI) is portioned into areas (sub-ROIs) that are characterized by different sets $\{f_1, f_2, f_3, f_4\}$, corresponding to different textures. More specifically a ROI is iteratively decomposed into 4 quadrants (sub-ROIs) on the basis of the difference among the values of the four features above (fig.2). The decomposition carries on iteratively for each sub-ROI until either the above differences are all below a threshold value (2nd condition of the block diagram: *Predicate Function and Threshold Parameter*) or the sub-ROI size is equal to \mathcal{L} , where ℓ is the side of the smallest square area resolvable by the diagnostic system (1st condition of the block diagram: *Step Dimension*).

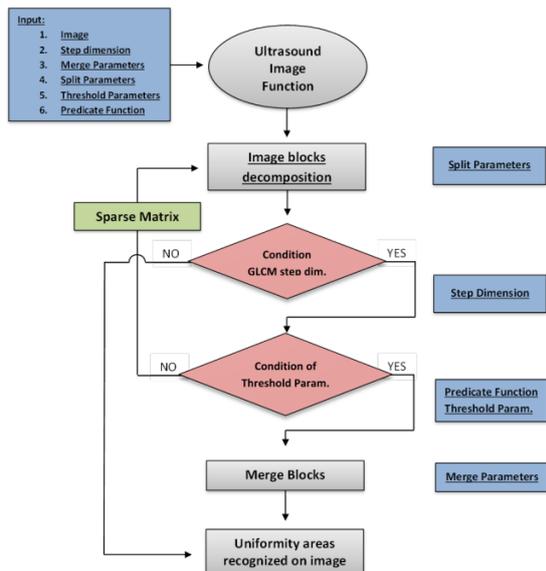


Fig. 1. Block diagram of the sparse matrix algorithm.

The GLCM features are compared between ROI quadrants on the six directions showed in Figure 2. Finally, depending on the Haralick features that have been considered for the merge operation, the sparse matrix obtained is solved to get the final decomposition: the corresponding image is subdivided into several areas of different uniformity values (Fig.3).

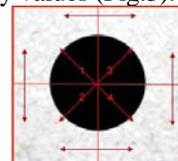


Fig. 2. Example of the directions taken into account for the comparison between features in the four quadrants, i.e. along horizontal, vertical and diagonal orientations.

In order to give a visual example of segmentation operation applied by the algorithm, in the following figure 3 two images, and their segmentation areas, are shown.

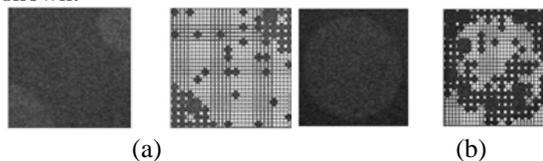


Fig. 3. Examples of outcomes of the segmentation procedure. (a) three and (b) two areas with different speckle pattern.

D. Dataset used for Uniformity algorithm tests

In this study, three datasets are used for testing the proposed method: 1) synthetic images, 2) real images from a same ultrasound scanner at different compression and gain settings, 3) real images from different commercial diagnostic systems and affected by different non-uniformities. The synthetic images (Circles Image Test Set or CITS) are of 128x128 pixelsize and produced by the MatLab 2014 software. In particular, six classes of images with circles at different size (i.e. 2, 4, 6, 16, 18 and 30 pixel radius respectively) and speckle noise level have been tested (figure 4), as circles can be associated to different non uniformities in medical practice (e.g. hepatoma - hepatocellular carcinoma).

A second image dataset contains vertical black band (Stripes Image Test Set or SITS), as they can be associated to non uniformities due to broken piezoelectric elements in the ultrasound probes. The images are collected at different Compression settings (i.e. 30, 45 and 60) and Gain level (i.e. range 50%-100% in steps of 5%) by means of a Philips iE33 ultrasound system, equipped with a phased array probe, i.e. Philips S8-3, that has been applied to a CIRS model 047 ultrasound phantom (fig. 5).

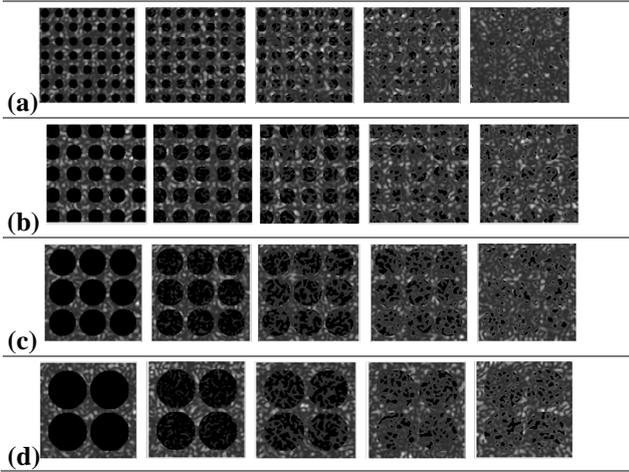


Fig. 4. Synthetic image dataset (circles dataset or CTS). Example of test images with circles of different size and speckle noise level (increasing from left to right). (a) 2px radius (b) 6px radius (c) 18px radius (d) 30 pixel radius

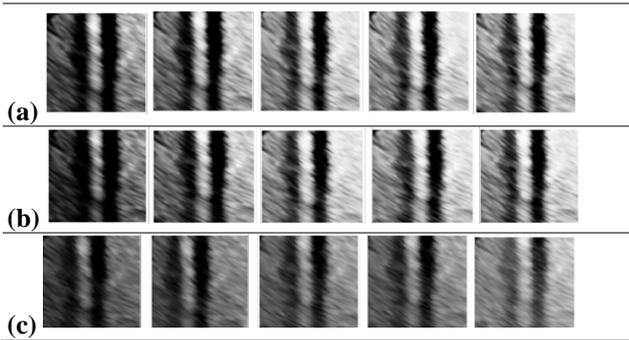


Fig. 5. Example of the 128pxx128px test images from the second dataset at different compression settings and gain level (SITS). (a) Compression settings 30 (maximum compression), (b) Compression settings 45 and (c) Compression settings 60 (minimum compression). Gain level ranges from 50% (1st column on the left) to 100%.

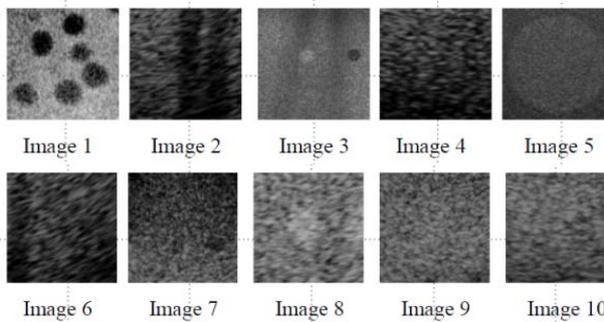


Fig. 6. Uniformity Image Test Set (UITS).

In figure 5 test images are of the same size, i.e. 128pxx128px, and collected at the same transmit power (i.e. maximum), position and field of view (i.e. 13 cm) in the ultrasound image. Finally, the algorithm per-

formances have been tested on a set of ultrasound images (Uniformity Image Test Set or UITS) acquired from different commercial diagnostic systems and affected by different non-uniformities (Fig. 6).

IV. RESULTS AND DISCUSSIONS

On the CITS the software recognition capability has been tested depending on the non-uniformities size, number and speckle noise level: in table 1 the corresponding uniformity values are reported.

Table 1. Uniformity values (%) for the synthetic image dataset (CITS) at different Speckle Noise Level. Relative uncertainties of the method ranges up to 28%

Circle radius size (px)	Speckle Noise lev.1	Speckle Noise lev.2	Speckle Noise lev.3	Speckle Noise lev.4	Speckle Noise lev.5
r = 2	1	1	2	36	75
r = 4	1	1	5	61	75
r = 6	2	3	58	61	75
r = 16	1	7	16	61	88
r = 18	3	3	54	58	75
r = 30	3	22	35	65	65

In particular for low speckle noises within the objects (Level 1, 2 and 3), the method provided low values of Uniformity, likely due to the detection of non uniformity areas into the image. On the other hand, the uniformity values increase with the speckle noise level and the size of not-uniformities. In order to consider the method outcomes depending on Compression and Gain settings, results for SITS are evaluated and shown in table 2.

Table 2. Uniformity values (%) at different compression and gain settings. Relative uncertainties of the method ranges up to 28%

Gain	Comp.sett ings 30	Comp.sett ings 45	Comp.sett ings 60
55%	34	54	34
60%	38	58	46
65%	46	60	52
70%	57	62	55
75%	54	62	62
80%	60	61	61
85%	61	65	60
90%	58	59	62
95%	62	61	60
100%	58	60	61

In particular, no significant differences have been found depending on the compression: all differences are below 12% (they are below 4% in most cases), that is less

than the estimated uncertainty of the method, i.e. 28%. Anyway, the outcomes seem reasonable as the black bands are clearly visible in all test images and the segmentation follow the band geometry also in the worst cases, where the images are almost black because of the low gain settings (figure 7).

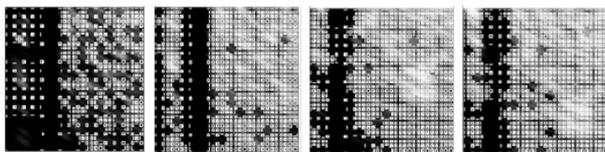


Fig. 7. Example of areas segmentation of black bands image.

Table 3. Uniformity values: Algorithm U_A compared with Human response U_H (Tests for Visual Uniformity assessment). Relative uncertainties of the U_A ranges up to 28%

UITS	U_A (%)	U_H (%)
1	1	11 ± 6
2	38	24 ± 11
3	46	39 ± 16
4	65	47 ± 7
5	27	50 ± 25
6	58	50 ± 8
7	62	59 ± 15
8	82	65 ± 8
9	53	88 ± 18
10	75	89 ± 7

In table 3, for most of the images in fig. 7 the algorithm outcomes U_A suggest a good agreement with the mean judgment U_H expressed by 7 human observers on the UITS, i.e. most of the differences between uniformity values are below 40% referred to the human judgment, half of them is below 30%, while U_A relative uncertainties have been estimated to range up to 28% [9]. Nevertheless, some differences can be significant: since the uniformity values are derived from considering all the features, it is reasonable that some of them have predominant behavior and decrease (or increase) the value of the uniformity measurement U_{ROI} also for images where patterns may be considered more (or less) homogenous by the human observers, i.e. max correlation. On the other hand, differences between U_A and U_H are likely due also to the unexperienced judgement of

the observers engaged in the test, as it can be confirmed by the high uncertainties of U_H .

V. CONCLUSIONS

In this work, an image segmentation method for Uniformity Quality assessment in diagnostic ultrasound is reported with some results. Most of the algorithm outcomes are in agreement with the judgment of 7 human observers on an image test set from commercial ultrasound scanners but, despite the encouraging outcomes (most of the differences are below 40%), further work is required to improve the method, its robustness and characterization. In particular, more tests should be done, also with different reference images, to better estimate the uncertainty of the method depending on the numerous variables (orientations and inter-pixel distances in GLCM calculation, discrimination thresholds, ROI characteristics,) and to provide a robust reference scale based on the judgment of experienced observers. Moreover, an in-depth study on algorithm sensitivity to non-uniformities and its relationship with the Haralick features should be conducted.

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