

# Characterization of interior permanent magnet synchronous motors for loss model algorithm identification

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**Abstract** – The paper provides the results of a detailed experimental study on the variations of the characteristics of an interior permanent magnet synchronous motor, when load, speed and/or magnetization conditions vary. In particular, the characterization is carried out by assessing, for several working conditions, the motor parameters that influence its efficiency. From the knowledge of the variability of these parameters, it is possible to develop a dynamic model of the motor, which accurately describes its behaviour and allows estimating the power losses for whatever speed and load. In order to validate the model, the values of the power losses obtained by using the model are compared with the values measured with experimental tests.

The study shows that it is possible to maximize the motor efficiency just acting on the direct axis current component, and therefore, it can be considered a first step towards the definition of a loss model algorithm for a control drive system able to minimize in real-time the power losses of the motor.

**Keywords** – interior permanent magnet synchronous motors, power loss minimization, speed control drive systems.

## I. INTRODUCTION

The interior permanent magnet synchronous motors (IPMSMs) are more and more employed in several low/medium power industrial drive applications. Their wide spread is due to their better performances with respect to the traditional synchronous and asynchronous motors; in particular the IPMSMs have higher power factor, higher torque/weight ratio and higher

power/current ratio. Moreover, these good performances continuously increase thanks to several implementations of new speed and torque control strategies.

Some of these strategies take into account the power losses minimization of the motor and, consequentially, the maximization of its efficiency for different working conditions. The most diffused losses minimization approaches presented in the literature can be classified in two main categories [1-8]: the “loss model control” and the “search control”. The first strategy involves the energy losses estimation from a mathematical model during the operation of the motor, while the second strategy consists of a step-by-step change of a control variable and a real-time measurement of the active power of the motor. However, most of these algorithms discussed in literature do not take into account all of the possible variations of the parameters of the IPMSM model [9-13].

This paper presents an experimental characterization of an IPMSM finalized to build an accurate dynamic model of the motor, which allows estimating the power losses for whatever speed and load, taking into account the variation of the motor parameters that influence its efficiency.

To perform the task, we carried out a series of experiments, measuring, for several working settings, the motor parameters that have an impact on its power losses. In particular, we evaluated the direct and quadrature axis inductances, the flux generated by the permanent magnets, the armature resistance and the resistance that symbolises the iron losses.

In a second stage of measurement, we directly measured the power losses varying load, speed and magnetization conditions. The comparison of the results of these measurements with the values of the power losses obtained by using the model was used to validate the proposed approach.

## II. DESCRIPTION OF THE METHOD

The starting point of our study is a well-known IPMSM model presented in several literature studies as a ‘‘circuitual approach’’ [14–18].

The model is based on the hypothesis of linearity and isotropy of the magnetic material (stator and rotor iron), sinusoidal distribution of the magneto-motive force in the air gap and negligible eddy currents. By referring to a d–q coordinate system, the equations that describe the IPMSM dynamic model are:

$$v_d = R i_d + L_d \frac{di_d}{dt} - p\omega L_q i_q \quad (1)$$

$$v_q = R i_q + L_q \frac{di_q}{dt} + p\omega L_d i_d + p\omega \psi_{PM} \quad (2)$$

$$T_m = T_r + F\omega + J \frac{d\omega}{dt} \quad (3)$$

$$T_m = \frac{3}{2} p [\psi_{PM} i_q + (L_d - L_q) i_d i_q] \quad (4)$$

where:

- $v_d$  and  $v_q$  are the direct and quadrature axis components of the stator phase voltages;
- $i_d$  and  $i_q$  are the direct and quadrature axis components of the stator phase currents;
- $p$  is the number of pole pairs;
- $\omega_m$  is the angular speed of the motor;
- $\Psi_{PM}$  is the flux generated by the permanent magnets;
- $R$  is the resistance of the three-phase stator winding;
- $L_d$  and  $L_q$  are the direct and quadrature axis inductances;
- $T_r$  is the load torque;
- $F$  is the coefficient of viscous friction;
- $J$  is the moment of inertia of the rotating parts.

From these equations, it is possible to calculate the power losses  $\Delta P_{tot}$ . However, in order to carry out an accurate estimation, it is necessary to take into account the variation of the motor parameters that influence its efficiency. In particular, the direct and quadrature axis inductances,  $L_d$  and  $L_q$ , and the flux of the rotor magnets  $\Psi_{PM}$  depend on the magnetic saturation, mainly in the motors with little air-gap and high magnetic flux [11,19,20]. The variation of these parameters is generated by the armature reaction and, therefore, its effect is bigger for high value of angular speed and load.

In order to make our model more accurate, we took into account also the variability of the resistance  $R_C$  representing the iron losses, which depends on the rotor speed. As regards the armature resistance  $R$ , which depends on its temperature, it is possible to neglect its variability, if we consider the stator in a thermal steady state.

## III. TESTS FOR THE MEASUREMENT OF THE MOTOR PARAMETERS

To carry out the measurement of the aforementioned parameters, we set up a test bench (fig. 1) composed of:

- a three-phase, six-pole brushless machine (Magnetic S.r.l., type BLQ-40), with SmCo permanent magnets (HITACHI Inc., type H-18B, with maximum specific energy equal to 143 kJ/m<sup>3</sup>). The stator winding is a three-phase, double-layer, shortened pitch, located into 27 slots. Table I reports the main rated values and parameters of the machine under test;

Table 1. Rated values and parameters of the IPMSM under test

Voltage	132 V
Current	3.6 A
Speed	4000 rpm
Torque	1.8 N·m
Number of pole pairs	3
Average stator resistance $R$	2.20 $\Omega$
Direct-axis inductance $L_d$	7.50 mH
Quadrature-axis inductance $L_q$	11.00 mH
PMs flux $\Psi_{PM}$	0.084 Wb
Coefficient of viscous friction $F$	0.001 N·m·s
Inertia moment $J$	0.001 kg·m <sup>2</sup>

- a DPS 30-A power converter (Automotion Inc.), directly connected to the electrical grid;
- a dSPACE® rapid prototyping control board, in order to drive the IGBT bridge of the converter;
- a HD-715 hysteresis brake (Magtrol Inc.), which allows to perform experimental tests at different load conditions
- a DSP6001 high-speed programmable dynamometer controller (Magtrol Inc.), used to drive the brake;
- a PZ 4000 three-phase power analyzer (Yokogawa Inc), used to measure the electrical quantities in the various working conditions of the motor;
- an ARTUS resolver (type 26SM19 U452), which is connected to the motor shaft in order to measure the motor speed;
- a variable auto-transformer (Variac Inc.), used for the measurement of the stator winding parameters;
- a PC with the dSPACE®-based electrical drive user interface, which allows to perform the real-time control and the supervision of the main electrical and mechanical quantities of the proposed system.

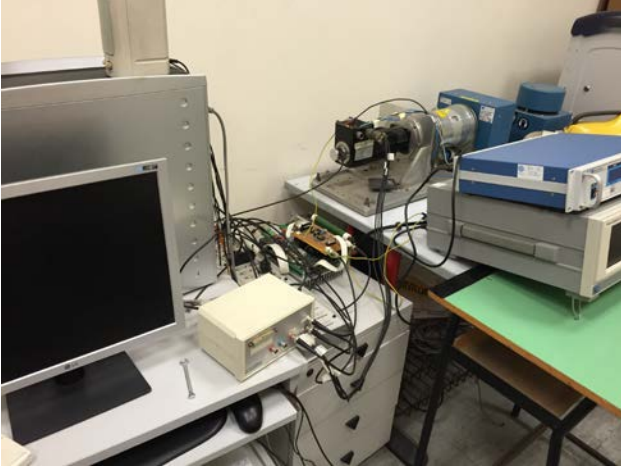


Fig. 1. IPMSM test bench

The direct and quadrature axis inductances were evaluated by means of blocked rotor tests. We measured the  $L_d$  for various  $i_d$  values, blocking the rotor at the  $0^\circ$  position, and the  $L_q$  for various  $i_d$  values, blocking the rotor at the  $90^\circ$  electrical position. Fig. 2 shows how the stator windings are connected to the measurement system.

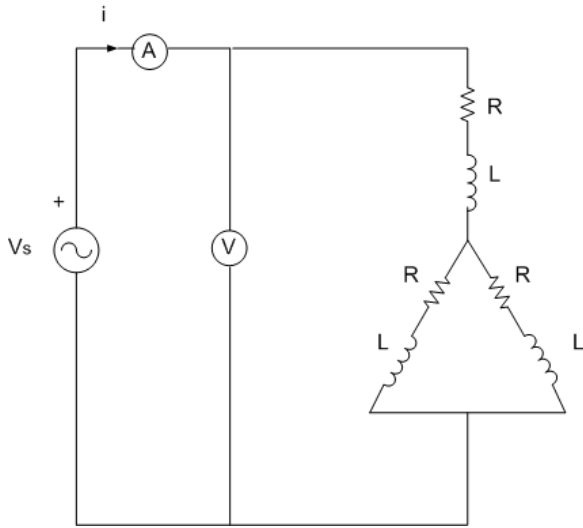


Fig. 2. Schematic for the measurement of  $L_d$  and  $L_q$

The  $L$  values were calculated by means of Eq. (5).

$$L = \frac{2}{3} \frac{\sqrt{Z^2 - R^2}}{2\pi f} \quad (5)$$

In fig. 3 and in fig. 4, the direct and quadrature axis inductances, as functions of  $i_d$  and  $i_q$  respectively, are reported.

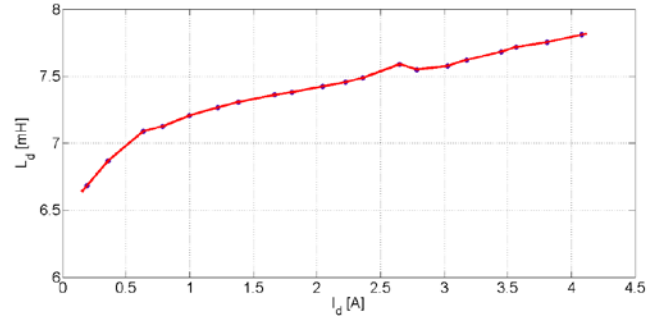


Fig. 3. Direct axis inductance as a function of  $i_d$

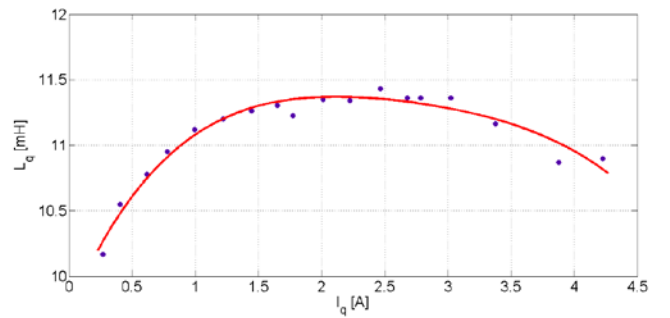


Fig. 4. Quadrature axis inductance as a function of  $i_q$

In order to evaluate the magnetic flux variability, we performed other blocked rotor tests, fixing the rotor position at the  $90^\circ$  electrical position and, therefore, setting  $i_d = 0$ . The torque  $T_m$  was measured by means of the dynamometer for various  $i_q$  values. Starting from Eq. (4), the flux value is given by:

$$\psi_{pm} = \frac{2 T_m}{3 p i_q} \quad (6)$$

The fig. 5 reports the magnetic flux trend versus  $i_q$ .

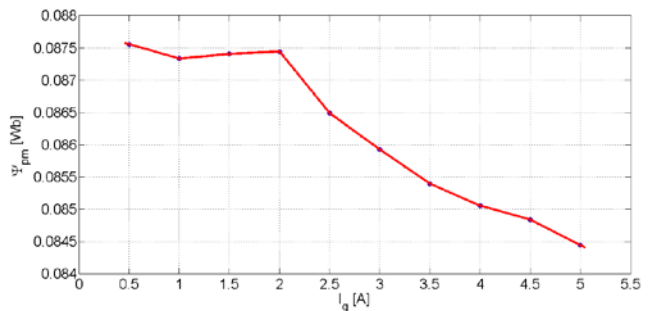


Fig. 5. Magnetic flux as a function of  $i_q$

The assessment of the resistance  $R_C$  representing the iron losses was carried out by means of no-load tests, varying the motor speed. In these conditions, the motor power consumption  $P_{tot}$  is:

$$P_{tot} = \Delta P_{fe} + \Delta P_{cu} + \Delta P_m + \Delta P_{add} \quad (7)$$

where:

- $\Delta P_{fe}$  are the losses in the stator and rotor iron;
- $\Delta P_{cu}$  are the joule losses in the stator winding that were calculated as  $3RI$  where  $R$  is the armature resistance and  $I$  is the current of each stator winding;
- $\Delta P_m$  are the mechanical losses (friction and ventilation) that were evaluated by means of a deceleration test;
- $\Delta P_{add}$  are the additional losses, which, in this context, can be neglected.

Therefore, by measuring the motor input electric power and rearranging the Eq. (7), it is possible to calculate the iron losses for various motor speeds. The values of the resistance  $R_C$  representing the iron losses were obtained from Eq. (8):

$$R_C = \frac{V^2}{\Delta P_{fe}} \quad (8)$$

The fig. 6 shows the  $R_C$  trend as a function of the rotor speed  $\omega_m$ .

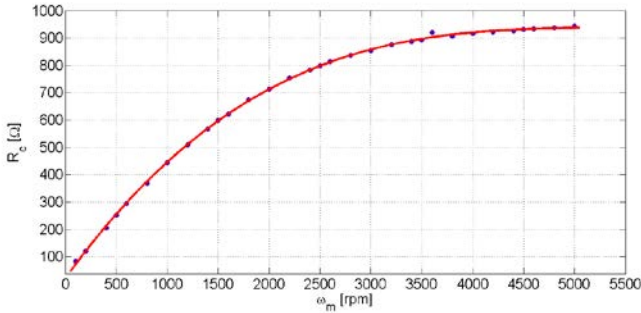


Fig. 6.  $R_c$  as a function of the rotor speed

Considering the variability of these four parameters and by means of the dynamic model of the motor, it is possible to evaluate the power losses for whatever speed and load.

#### IV. TESTS FOR THE DIRECT MEASUREMENT OF THE MOTOR LOSSES

In order to validate the model, the values of the power losses  $\Delta P_{tot}$  obtained by using the model (with both constant and variable parameters) were compared with the values obtained by experimental tests measuring the power losses as difference between the electrical input power and the mechanical output power [21-22]. The losses were

measured for 1000 different working conditions, varying: the motor speed in the range  $500 \div 4000$  rpm with steps of 500 rpm; the load in the range  $0 \% \div 100 \%$  of rated load with steps of 25 %; the  $i_d$  value in the range  $-2.4 \div 2.4$  A with steps of 0.2 A. The expanded uncertainty ( $k = 2$ ) of the  $\Delta P_{tot}$  measurements is 1.2 % [23].

For instance, fig. 7, 8 and 9 show this comparison in three different working conditions, reporting the losses evaluated with the constant parameters model (blue lines), the losses evaluated with the variable parameters model (red lines) and the losses measured with the experimental tests (black lines).

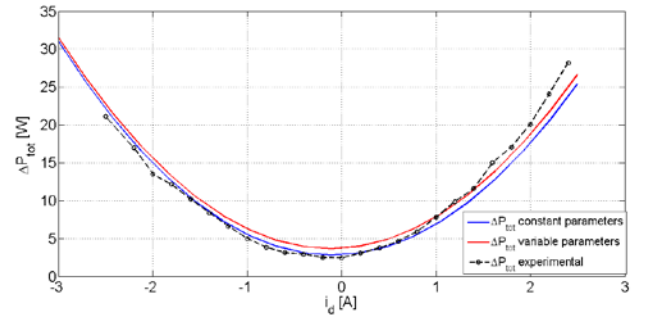


Fig. 7. Comparison between the losses evaluated with the model and the measured losses (1500 rpm; no-load)

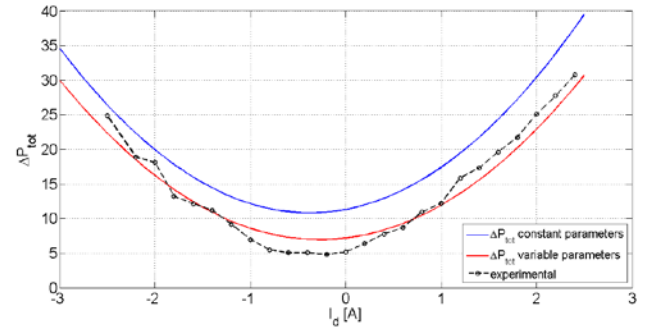


Fig. 8. Comparison between the losses evaluated with the model and the measured losses (3000 rpm; no-load)

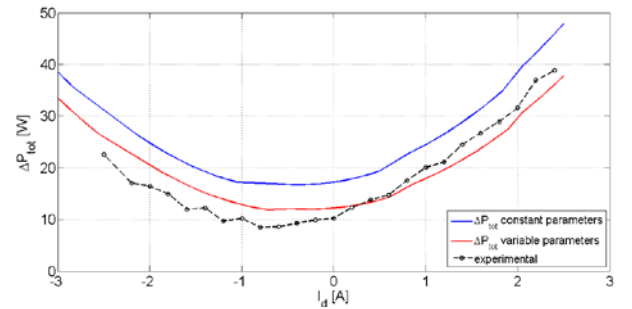


Fig. 9. Comparison between the losses evaluated with the model and the measured losses (3000 rpm; 50 % load)

It is possible to notice that considering the variability of the motor parameters leads to a more accurate assessment of the motor losses rather than using a constant parameters model. As could be expected, the differences gets bigger, as the motor speed and/or load increase.

Fig. 10 reports the IPMSM efficiency parametrized for different speeds, as function of  $i_d$  with an applied load fixed at 25 % of the rated one. The maximum efficiency is obtained for negative values of  $i_d$ . In addition, by increasing the speed, the related peak is detected for higher negative values of  $i_d$ .

Fig. 11 reports the IPMSM efficiency parametrized for different loads, as function of  $i_d$  when the motor is rotating at 2000 rpm. The maximum efficiency is obtained when the motor works between 25% and 50% of the full load.

It is possible to notice that, for each operating condition of the motor, it is always possible to determine a specified  $i_d$  value that maximizes the IPMSM efficiency without decreasing the dynamic performances of the drive.

The good agreement of the two graphs validates both the exactness of the model and the measurement accuracy of the motor parameters.

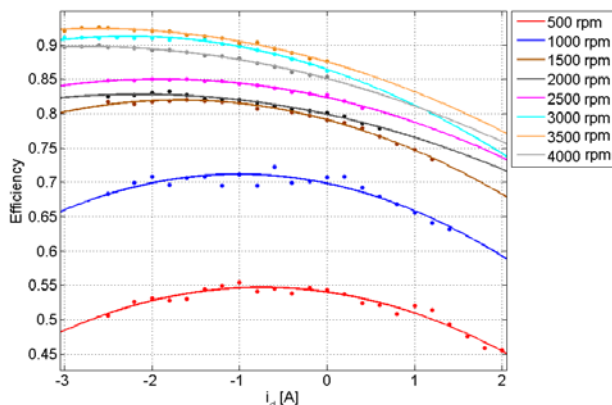


Fig. 10. IPMSM efficiency as a function of  $i_d$  (25 % of rated load)

## V. NOVELTIES IN THE PAPER

Several loss model algorithms were presented in literature. However, most of them do not completely consider the variations in terms of frequency and saturation of all the parameters involved in the dynamic model of the machine.

In this paper, the variability of all parameters, which have an impact on the power losses of the motor, is considered. In addition, the variability of these parameters is studied also for demagnetizing values of the direct-axis current component. Therefore, the proposed loss model algorithm allows a more accurate detection of the minimum point of the IPMSM power losses, both in terms of  $\Delta P$  and  $i_d$  values.

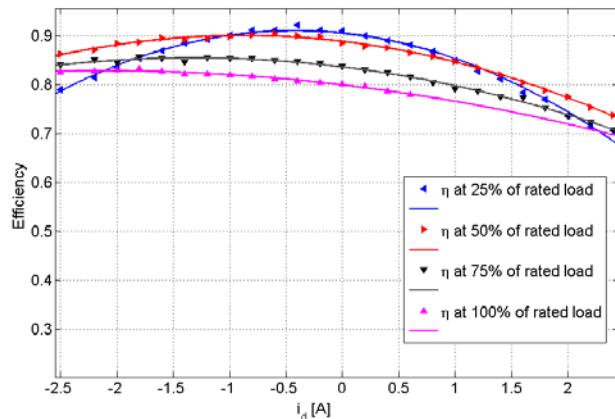


Fig. 11. IPMSM efficiency as a function of  $i_d$  (2000 rpm)

## VI. CONCLUSIONS

This paper presented an experimental study on the efficiency of an IPMSM at different working and magnetization conditions.

Starting from a well-known dynamic model of the motor, the variability of the model parameters, on which the power losses depend, was studied and evaluated. By taking into account these variabilities, it was possible to sharpen the dynamic model and to obtain a more accurate estimate of the power losses of the motor.

The validity of the model was proved by comparing the power loss estimates with the loss values obtained from experimental tests, directly measuring the power losses as difference between the electrical input power and the mechanical output power.

The results of the study demonstrate that the motor efficiency can be maximized for any IPMSM working condition by simply acting on the direct axis current and without decreasing the dynamic performances of the electrical drive.

Because of its high flexibility, the proposed approach is applicable to several typologies of brushless motors and their related applications.

## VII. ACKNOWLEDGMENT

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## REFERENCES

- [1] S. Vaez, V. John, and M. Rahman, "Adaptive loss minimization control of inverter-fed ipm motor drives," in Power Electronics Specialists Conference, 1997. PESC '97 Record., 28th Annual IEEE, vol. 2, pp. 861–868 vol.2, Jun 1997.
- [2] C. Mademlis, J. Xypteras, and N. Margaritis, "Loss minimization in surface permanent-magnet synchronous motor drives," Industrial Electronics,

- IEEE Transactions on, vol. 47, pp. 115–122, Feb 2000.
- [3] F. Fernandez-Bernal, A. Garcia-Cerrada, and R. Faure, “Model-based loss minimization for dc and ac vector controlled motors including core saturation,” in Industry Applications Conference, 1999. Thirty-Fourth IAS Annual Meeting. Conference Record of the 1999 IEEE, vol. 3, pp. 1608–1615 vol.3, 1999.
- [4] A. Bazzi and P. Krein, “Review of methods for real-time loss minimization in induction machines,” Industry Applications, IEEE Transactions on, vol. 46, pp. 2319–2328, Nov 2010.
- [5] F. Azevedo and M. Uddin, “Recent advances in loss minimization algorithms for ipmsm drives,” in Industry Applications Society Annual Meeting, 2014 IEEE, pp. 1–9, Oct 2014.
- [6] A.O. Di Tommaso, R. Miceli, G.R. Galluzzo, and M. Trapanese, “Optimum performance of permanent magnet synchronous generators coupled to wind turbines” in 2007 IEEE Power Engineering Society General Meeting, PES.
- [7] A.O. Di Tommaso, R. Miceli, G.R. Galluzzo, and M. Trapanese, “Efficiency control for permanent magnet synchronous generators” in Proceedings of the IEEE International Conference on Industrial Technology, art. no. 4237887, pp. 2079-2084.
- [8] G. Cipriani, V. Di Dio, L.P., Di Noia, F. Genduso, D. La Cascia, R. Miceli, R. Rizzo, “A PV plant simulator for testing MPPT techniques” in 4th International Conference on Clean Electrical Power: Renewable Energy Resources Impact, ICCEP 2013, art. no. 6586921, pp. 483-489.
- [9] S. Morimoto, Y. Tong e Y. Takeda, “Loss Minimization Control of Permanent Magnet Synchronous Motor Drives”, IEEE Transactions on industrial electronics, vol. 41, no. 5, October 1994.
- [10] C. Mademlis e V. G. Agelidis, “On Considering Magnetic Saturation with Maximum Torque to Current Control in Interior Permanent Magnet Synchronous Motor Drives”, IEEE Transactions on energy conversion, vol. 16, no. 3, September 2001.
- [11] J. Lee, K. Nam e S. Choi, “Loss-Minimizing Control of PMSM With the Use of Polynomial Approximations”, IEEE Transactions on power electronics, vol. 24, no. 4, April 2009.
- [12] S. Vaez e J. Vilayil, “Minimum Loss Operation of PM Motor Drives”, IEEE Canadian Conference on , vol.1, no., pp.284-287 vol.1, September 1995.
- [13] J. Lee, K. Nam, S. Choi e S. Kwon, “A Lookup Table Based Loss Minimizing Control for FCEV Permanent Magnet Synchronous Motors”, in IEEE Vehicle Power and Propulsion Conference, Arlington, TX, pp. 175-179, 2007.
- [14] M. Fazil and K. R. Rajagopal, “Nonlinear dynamic modeling of a singlephase permanent-magnet brushless dc motor using 2-d static finiteelement results,” Magnetics, IEEE Transactions on, vol. 47, pp. 781–786, April 2011.
- [15] M. Hussin, M. Azuwir, and Y. N. Zaiazmin, “Modeling and validation of brushless dc motor,” in Modeling, Simulation and Applied Optimization (ICMSAO), 2011 4th International Conference on, pp. 1–4, April 2011.
- [16] O. Mohammed, S. Liu, and Z. Liu, “A phase variable model of brushless dc motors based on finite element analysis and its coupling with external circuits,” Magnetics, IEEE Transactions on, vol. 41, pp. 1576–1579, May 2005.
- [17] B. Kerdsup and N. Fuengwarodsakul, “Dynamic model of brushless dc drive using fe method based characteristics,” in Power Electronics and Drive Systems (PEDS), 2011 IEEE Ninth International Conference on, pp. 66–71, Dec 2011.
- [18] A. Matsumoto, M. Hasegawa, and S. Doki, “A novel ipmsm model for robust position sensorless control to magnetic saturation,” in Power Electronics Conference (IPEC-Hiroshima 2014 - ECCE-ASIA), 2014 International, pp. 2445–2450, May 2014.
- [19] K. Yu, H. Guo e Z. Sun, Efficiency Optimization Control of Permanent Magnet Synchronous Motor for Electric Propulsion System, Busan, Korea: 2013 International Conference on Electrical Machines and Systems, Oct. 26-29, 2013.
- [20] Z. Li and H. Li, "MTPA control of PMSM system considering saturation and cross-coupling," Electrical Machines and Systems (ICEMS), 2012 15th International Conference on, Sapporo, 2012, pp. 1-5.
- [21] M. Caruso, A. O. Di Tommaso, F. Genduso and R. Miceli, "Experimental investigation on high efficiency real-time control algorithms for IPMSMs," Renewable Energy Research and Application (ICRERA), 2014 International Conference on, Milwaukee, WI, USA, 2014, pp. 974-979.
- [22] M. Caruso, A. O. Di Tommaso, R. Miceli and C. Spataro, "Experimental study on efficiency enhancement in Interior Permanent Magnet Synchronous machines," Clean Electrical Power (ICCEP), 2015 International Conference on, Taormina, Italy, 2015, pp. 518-522.
- [23] C. Spataro, “ADC based measurements: A common basis for the uncertainty estimation” in Proceedings of 17th Symposium IMEKO TC 4, 3rd Symposium IMEKO TC 19 and 15th IWADC Workshop. p. 389-393, Kosice, Slovak Rep., 8-10 Sept. 2010.